



# **Nantonac Collaborative Filtering**

## **A Model-Based Approach**

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# Overview

Many prediction algorithms and user interfaces are developed for recommender systems

**BUT**

For collecting users' preference data, almost all systems use a **rating method** or a **scoring method**



We proposed to use a **Ranking method**

# Previous and New Contribution

Our previous contributions are...

- \* proposed to use a ranking method for collecting preference data
- \* developed a technique that enables to apply ranking data to existing recommendation algorithms designed for scores
- \* prediction accuracies are improved by using a ranking method in comparison with a scoring method

**BUT**

**Superiority of a ranking method is tested only for memory-based algorithms**



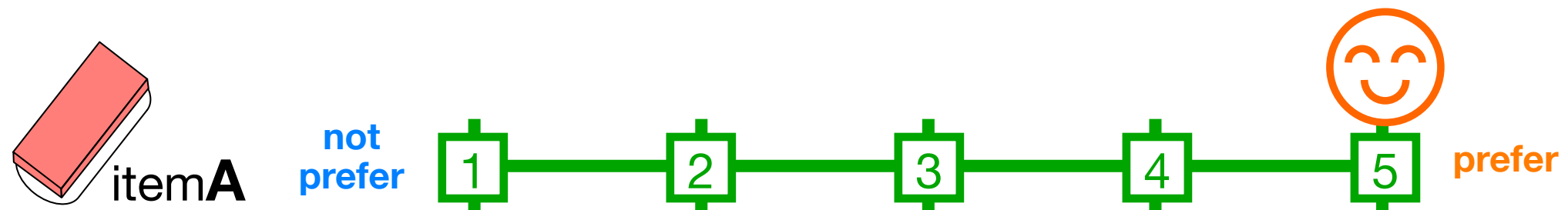
A ranking method is also **effective for model based algorithms: matrix decomposition and pLSA**



# Rating / Scoring Methods

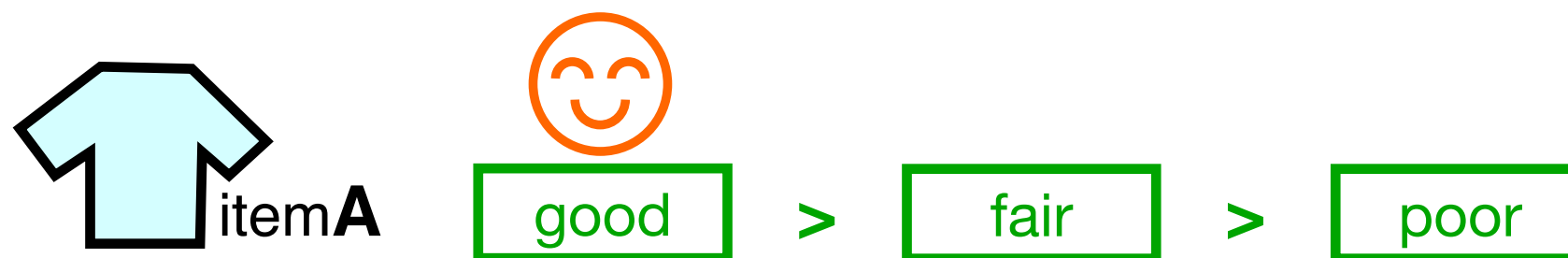
## Scoring Method

Items are evaluated by using scales with scores, s.g., a five-points-scale  
The user selects “5” in a five-point scale if she prefers the item A



## Rating Method

Items are evaluated by using ordered ratings, s.g., {good, fair, poor}  
The user selects “good” if she sets a high value the item A

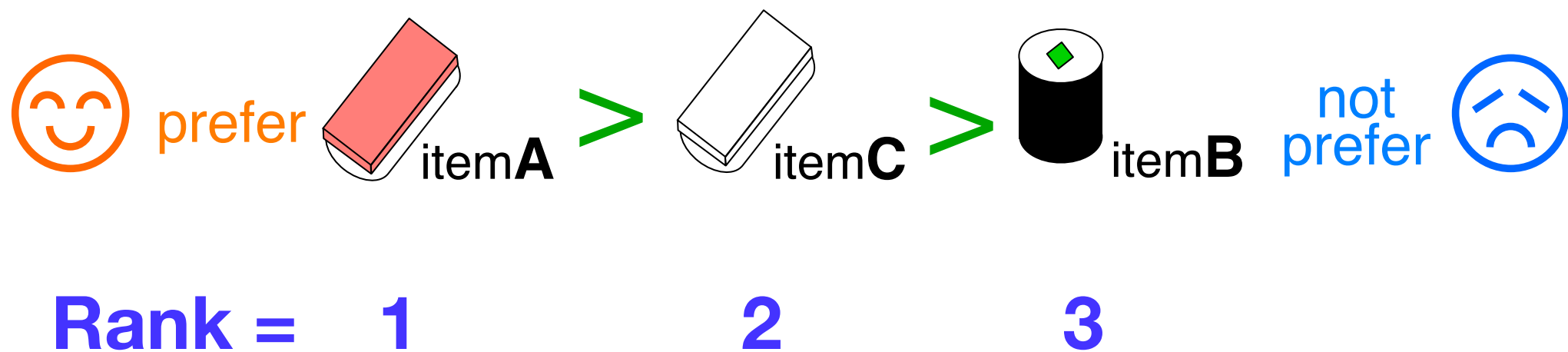


# Ranking Method

## Ranking Method

Objects are sorted according to the degree of preference

The user prefers the item A most, and the item B least



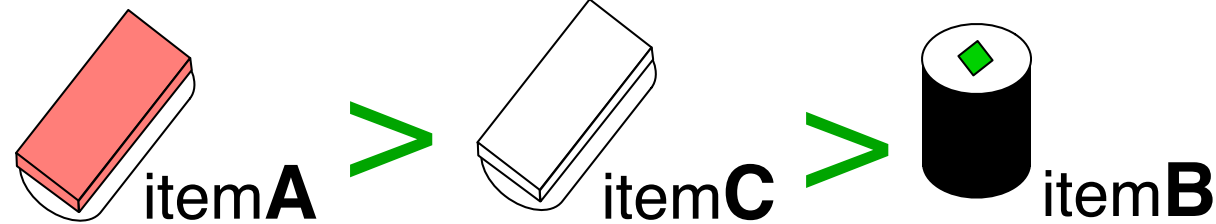


# Ranks to Scores

We developed a simple technique to convert ranks in preferential orders to preferential scores based on order statistics theory

$$\text{expectation of ranks in a unobserved complete order} \propto \frac{\text{rank in a observed order}}{(\text{length of a observed order}) + 1}$$

Example:



rank of item A is 1

length of observed order is 3

Set the score  $1/4 = 1 / (3 + 1)$  to the item A

# Assumption

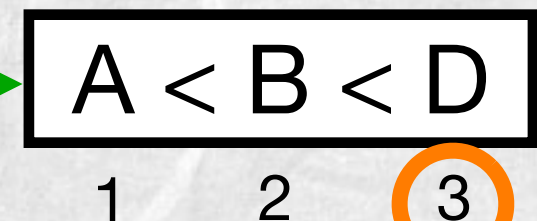
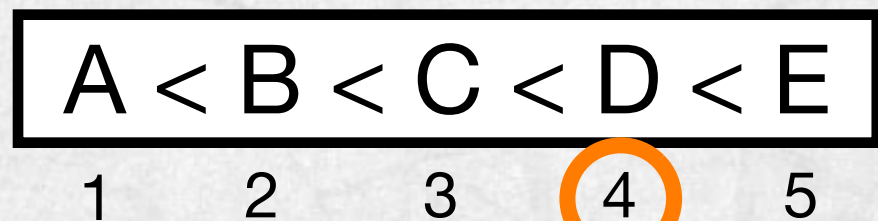
consisting of all possible objects and **unobserved**

consisting of sub-sampled objects and **observed**

**uniformly at random**

**unobserved**  
complete order

**observed**  
sample order



expectation of rank  
in a complete order

observed rank





# Interface

## WWW Interface for asking user preference by ranking method

もう一度、あなたが好きな順に番号をつけてください。

途中で、どのネタや番号を選んでいないか分からなくなったときには、「チェックする」ボタンを押すと、まだ選んでいない番号やネタが分かります。

チェックする

	1番	2番	3番	4番	5番	6番	7番	8番	9番	10番
とびこ	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
たい	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
とろ	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
まぐろ	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
いくら	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
めんたいこ	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
あおやぎ	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
しゃこ	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
うなぎ	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
赤貝	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
	1番	2番	3番	4番	5番	6番	7番	8番	9番	10番

終わったら押してください

「とびこ」 トビウオの卵  
「とろ」 まぐろの脂の多い部分  
「たい」 鯛  
「まぐろ」 鯖：赤身の部分

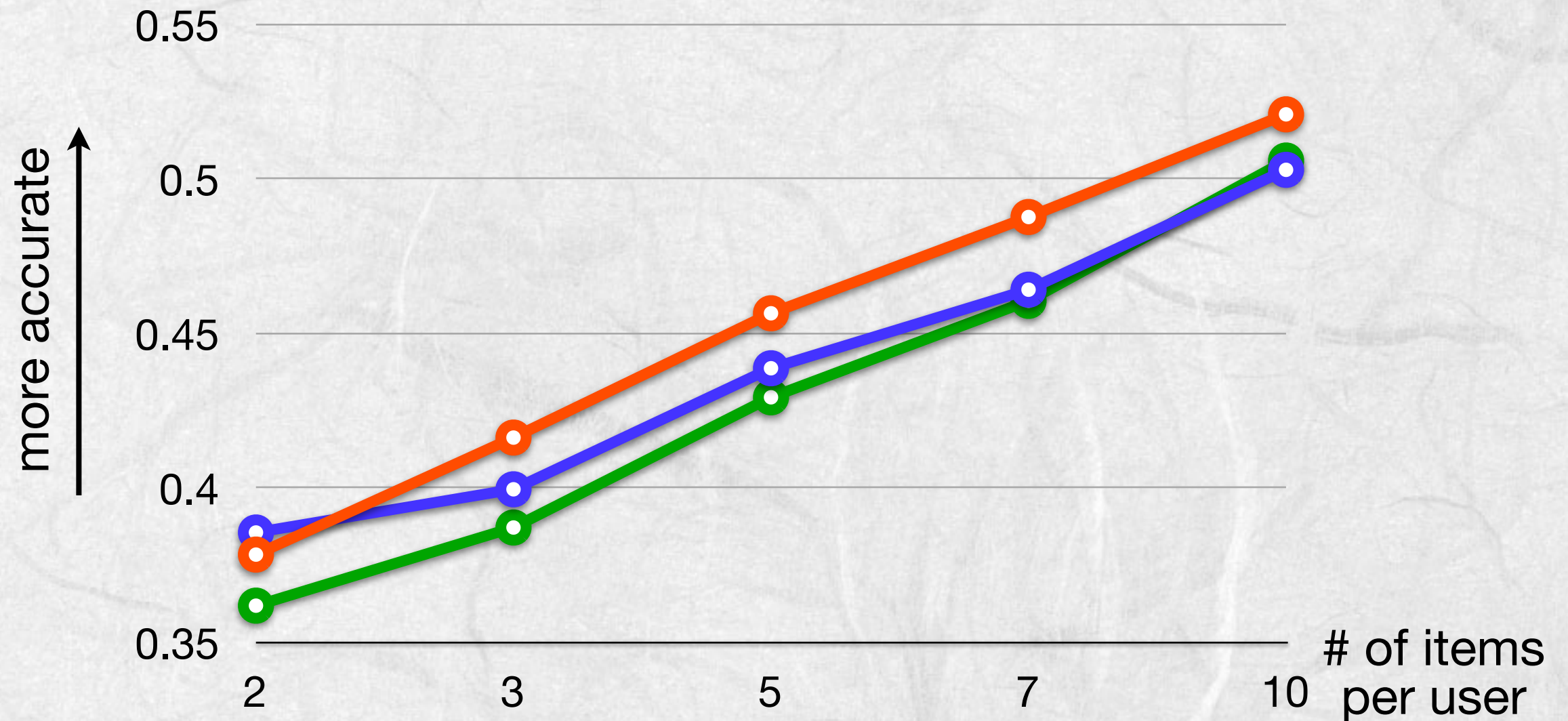
name of sushi

Specify Ranks

1. show 10 items to the user
2. the user specify all the rank of each items
3. press “submit” button
4. if error (ex. the same ranks are assigned to the two items) is detected, the system request to re-input



# Memory-Based Method



Grouplens like memory-based method

- ranking method + default voting
- scoring method + default voting + standardization (min-max range)
- scoring method + default voting + rank correlation



# Matrix Decomposition Model

The user x's score to the item y is estimated by the following Eq.

$$\hat{s}_{xy} = b + c_x + d_y + \mathbf{u}_y^\top \left[ \mathbf{v}_x + \frac{1}{\sqrt{|\mathcal{Y}_x|}} \sum_{y' \in \mathcal{Y}_x} \mathbf{w}_{y'} \right]$$

Annotations for the equation above:

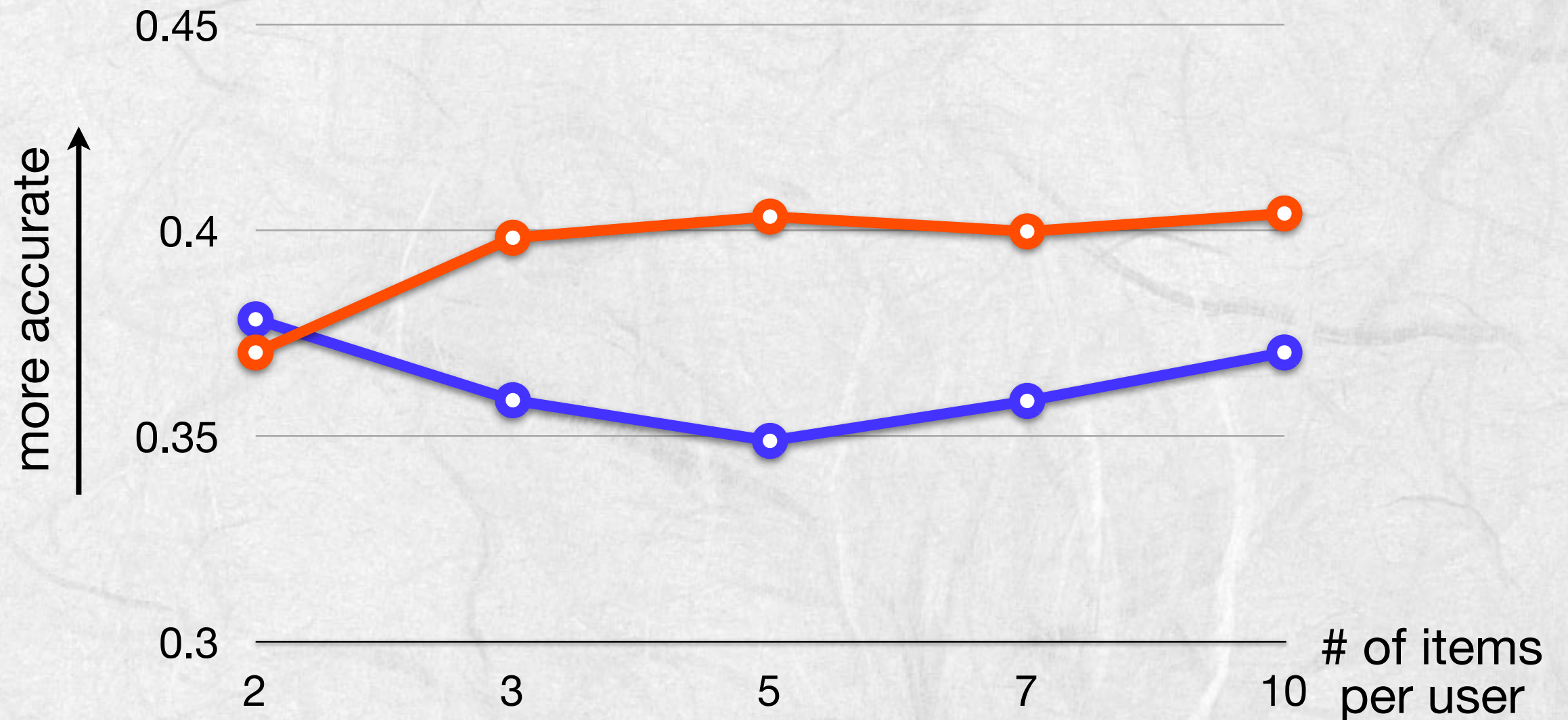
- overall bias (points to  $b$ )
- per item bias (points to  $d_y$ )
- per user bias (points to  $c_x$ )
- user x's cross effect vector (points to  $\mathbf{v}_x$ )
- information vector which items are rated (points to  $\mathbf{w}_{y'}$ )
- item y's cross effect vector (points to  $\mathbf{u}_y^\top$ )
- a set of items rated by user x (points to  $\mathcal{Y}_x$ )

Parameters are estimated by minimizing the loss function:

$$\text{loss}(\mathcal{D}; \Theta) = \sum_{(x,y,s) \in \mathcal{D}} (s_{xy} - \hat{s}_{xy})^2 + \lambda[\text{reg.term}]$$



# Matrix Decomposition Model



Memory-based method: Matrix decomposition

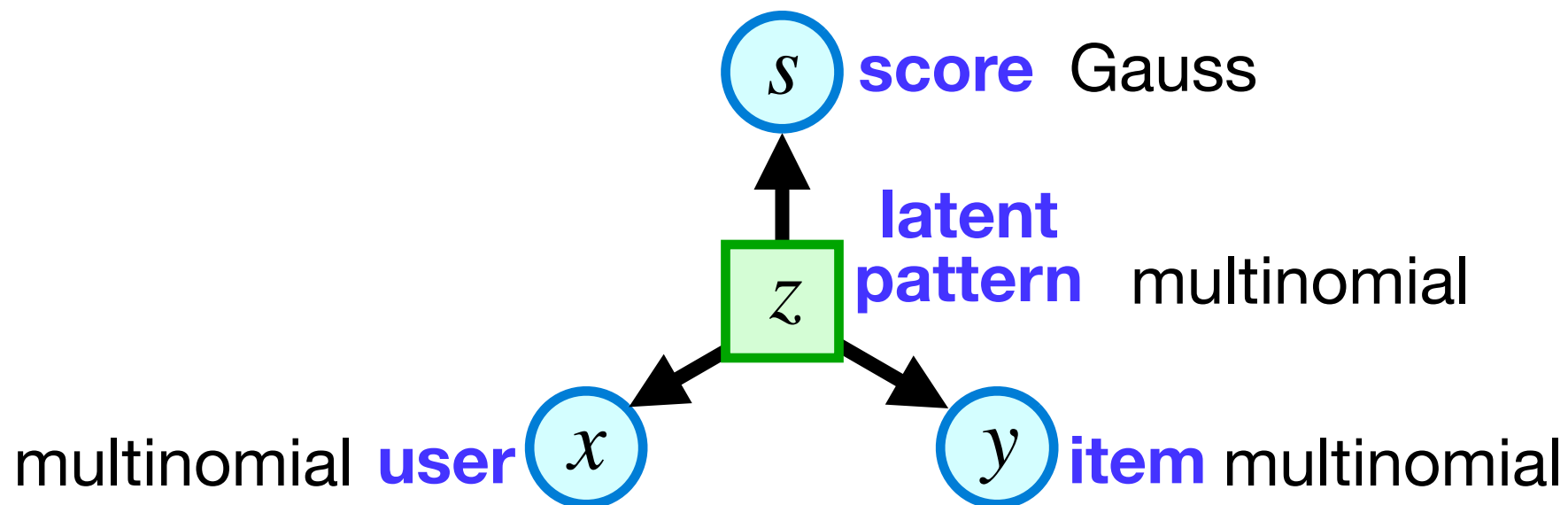
- ranking method + matrix decomposition
- scoring method + matrix decomposition



# pLSA-like Model

Hoffman's pLSA model is modified so as to deal with real scores

## Graphical model of our pLSA-like model

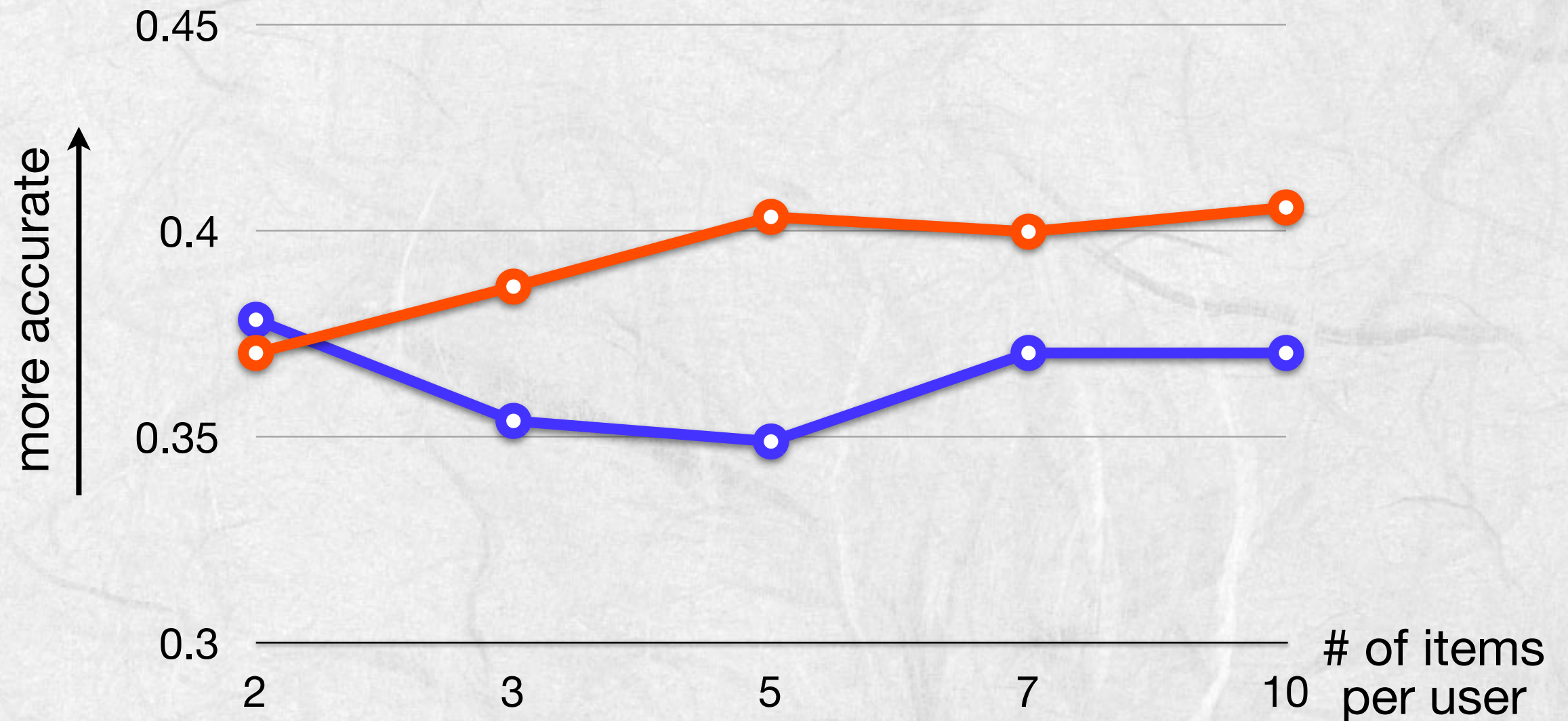


Parameters are estimated by maximizing the likelihood function

$$\mathcal{L}(\mathcal{D}; \Theta) = \sum_{(x,y,s) \in \mathcal{D}} \log \sum_z \Pr[z] \Pr[x|z] \Pr[y|z] \mathcal{N}(s; \mu_z, \sigma_z^2)$$



# pLSA-like Model

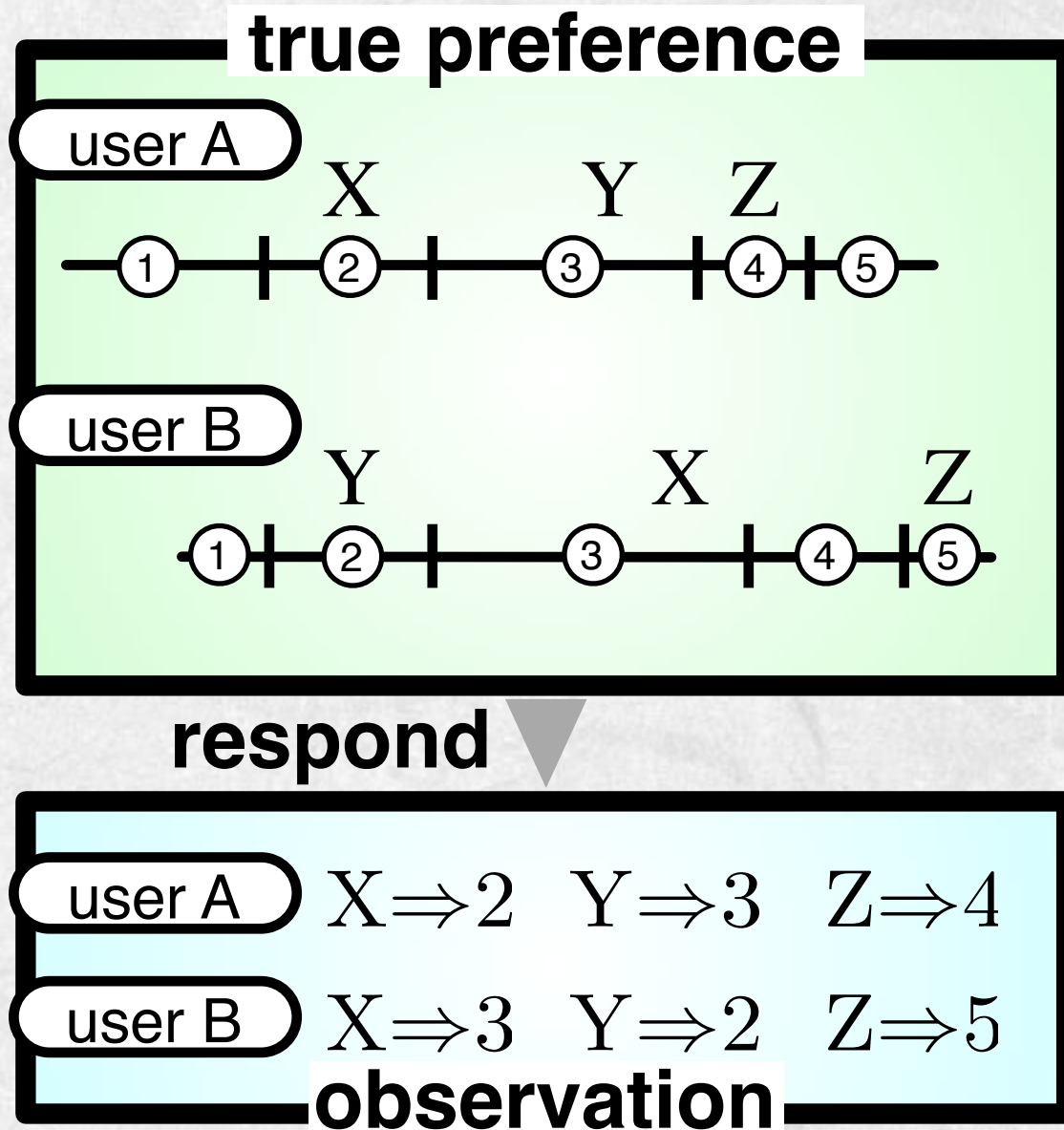


Memory-based method: Matrix decomposition

- ranking method + pLSA-like model
- scoring method + pLSA-like model



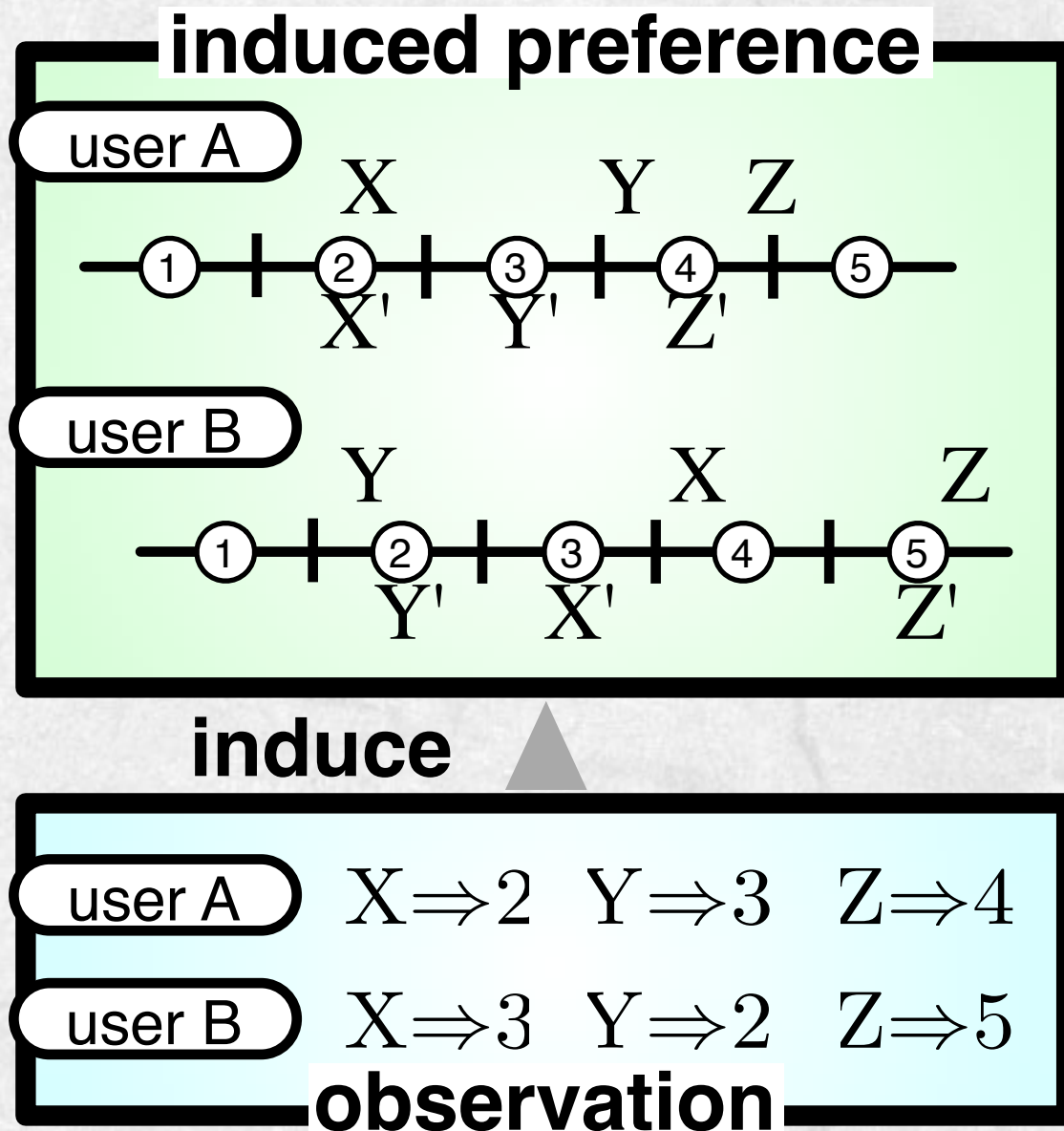
# Why Ranking performed better?



- ✿ The degree of true preference cannot be observed directly
- ✿ Each user uses one's own mapping from the degree to rating score
- ✿ Ex: The degree of preference on X lies in interval 2 of user A  
➔ User A replies rating score 2



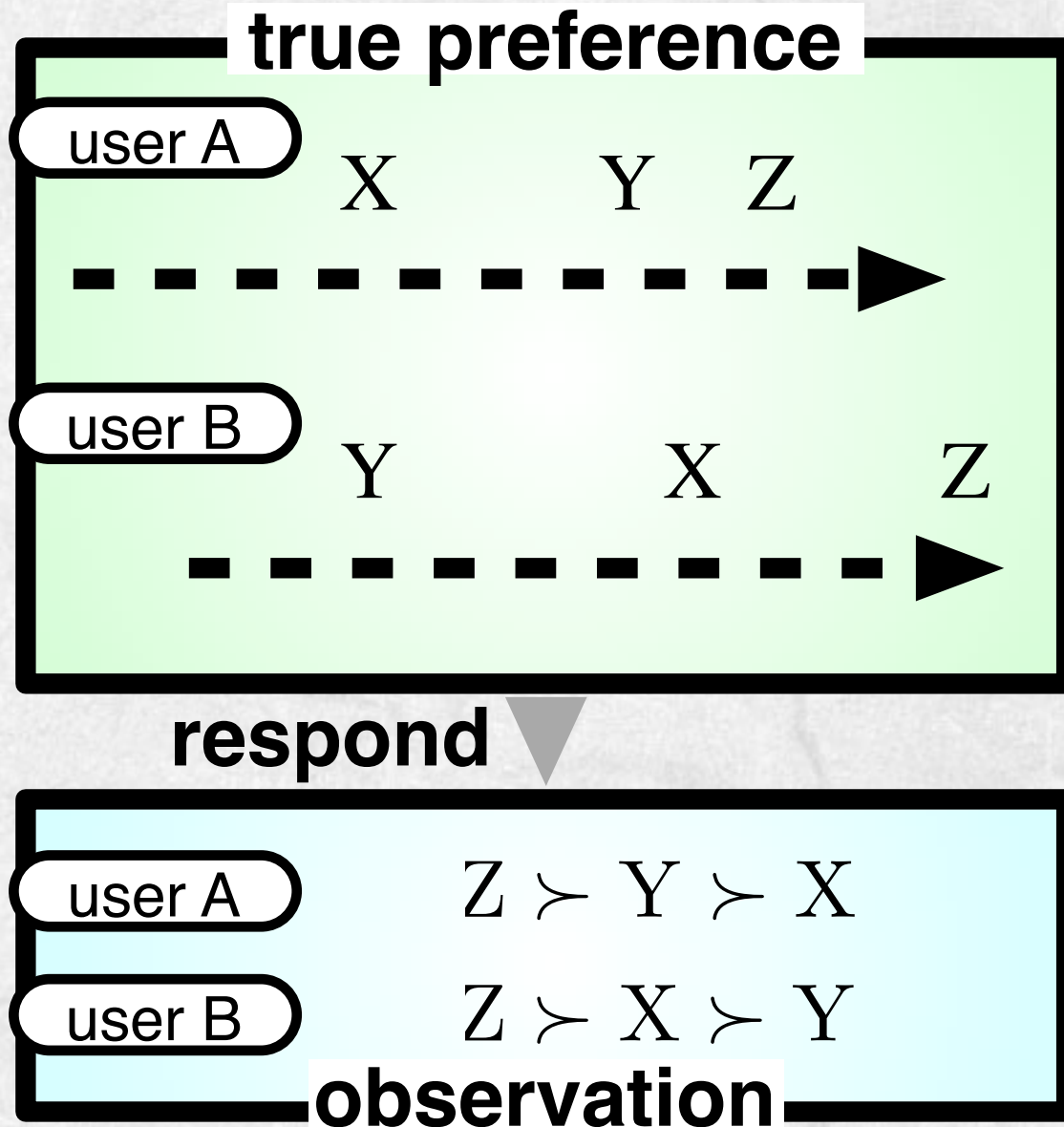
# Why Ranking performed better?



- ✿ We now want to induce the true degree of preference
- ✿ The true mapping to rating scores is unknown
- ✿ A common idealized mapping scale is of necessity used
- ✿ The induced degrees of preferences might not be true
- ✿ Ex: The true degrees of X, Y, and Z are changed to X', Y', and Z', respectively



# Why Ranking performed better?



- ✿ In a ranking method, the degrees of preferences are **relatively specified**
- ✿ We don't need to use a **unsafe groundless mapping** between the degrees of preference and observed rating scores



# Merits and Demerits of Ranking Methods

## Merits

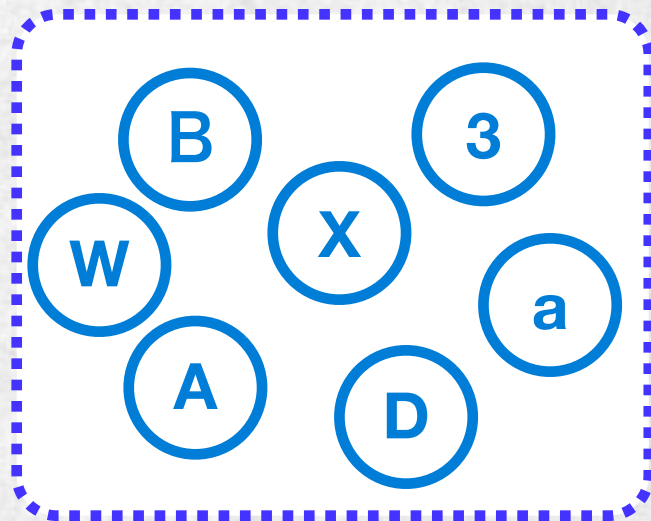
- ✿ **High consistency of preferences** between and within users

## Demerits

- ✿ **Less algorithms** for analysis are available
  - ➔ Develop new algorithms
- ✿ **Difficult to rate many items** at the same time
  - ➔ Subsets of items are sorted multiple times
- ✿ **Lack of absolute evaluation**

# Ranking Many Objects

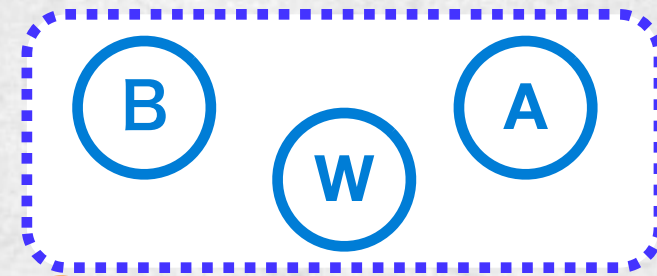
many objects



**Sort all objects  
AT THE SAME TIME**



sampling small sets of objects



user



sort these small  
sets of objects

**Iterate sampling  
and Sorting**





# Relevance Feedback

[Joachims 02, Radlinski+ 05]

Learning from relevance feedback is a typical absolute ranking task

## Ranked List for the query Q

1: document A

2: document B

3: document C

4: document D

5: document E

selected  
by user

The user scans this list from the top, and selected the third document C.

The user checked the documents A and B, but these are not selected.



This user's behavior implies relevance feedbacks:  $C > A$  and  $C > B$ .

Object ranking methods can be used to update document's relevance based on these feedbacks



# What's "Nantonac"

The word *nantonac* originates from a Japanese word, *nantonaku*, which means just somehow.

For example, in Japanese, if I say "I *nantonaku* understand something," I am saying that I cannot specifically explain why I understand it, but that I somehow do.

Order responses allow a more vague and intuitive expression of users' preferences, so we have named this method the *nantonac collaborative filtering*.



# Our Related Publications

## Our Related Publications

- ✿ T. Kamishima, "Nantonac Collaborative Filtering: Recommendation Based on Order Responses", Proc. of The 9th Int'l Conf. on Knowledge Discovery and Data Mining (KDD 2003)
- ✿ T. Kamishima and S. Akaho, "Nantonac Collaborative Filtering — Recommendation Based on Multiple Order Responses", Proc. of The Int'l Workshop on Data-Mining and Statistical Science (2006)

**Our SUSHI data sets are available at**

**<http://www.kamishima.net/sushi/>**